

CORRECTIONS - FIRST EDITION - MARCH 12 2007

1. Page 4, line -2: Replace “consequences” by “consequence”.
2. Page 8, add line 3: “All topological spaces in the sequel are assumed to be Hausdorff”.
3. Page 41, line 10: Normal(0,I) and not Normal(0,1).
4. Page 60, line -1: replace Π_λ by $\mathbf{\Pi}_\lambda$.
5. Page 61, line -4: should be “unique non negative left eigenvectors”.
6. Page 68, line 5: replace $H(q) \triangleq \dots$ by $H(q) \triangleq - \dots$
7. Page 84 line -2: not *necessarily*.
8. Page 86 line -11: replace $\Sigma = \mathbb{R}$ by $\Sigma = [0, 1]$.
9. Page 90, Theorem 3.6.8, part (a): add “for all sufficiently large n”
10. Page 111, line 17: Replace \mathcal{X} by \mathcal{Y} .
11. Page 130, line -13: Add “log” after the second equality to read

$$= \log \int_{\mathcal{X}} e^{\lambda(x)} \mu_\epsilon(dx), \quad \lambda \in \mathcal{X}^*,$$

12. Page 134, Figure 4.5.2: the lines are not of $\langle \lambda_i, x \rangle - g(\lambda_i) = 0$ but rather of $\langle \lambda_i, x \rangle - g(\lambda_i) = c_i$, where $c_i = f(x_i)$ and x_i is the point of tangency of the line with slope λ_i to the graph of $f(\cdot)$.
13. Page 152, line -10: replace

$$\mathcal{AC} \triangleq \left\{ \phi \in C([0, 1]) : \sum_{\ell=1}^k |t_\ell - t_{\ell-1}| \rightarrow 0 \implies \sum_{\ell=1}^k |\phi(t_\ell) - \phi(t_{\ell-1})| \rightarrow 0 \right\}.$$

by

$$\mathcal{AC} \triangleq \left\{ \phi \in C([0, 1]) : \sum_{\ell=1}^k |t_\ell - s_\ell| \rightarrow 0, s_\ell < t_\ell \leq s_{\ell+1} < t_{\ell+1} \implies \sum_{\ell=1}^k |\phi(t_\ell) - \phi(s_\ell)| \rightarrow 0 \right\}.$$

14. Page 156, line -4 until Page 157, line 4: Replace text by

Finally, suppose that $\phi \in \mathcal{X}$ and $\phi \notin \mathcal{AC}$. Then there exist $\delta > 0$ and $\{s_1^n < t_1^n \leq \dots \leq s_{k_n}^n < t_{k_n}^n\}$ such that $\sum_{\ell=1}^{k_n} (t_\ell^n - s_\ell^n) \rightarrow 0$, while $\sum_{\ell=1}^{k_n} |\phi(t_\ell^n) - \phi(s_\ell^n)| \geq \delta$. Note that, since Λ^* is nonnegative,

$$\begin{aligned} I_{\mathcal{X}}(\phi) &= \sup_{\substack{0 < t_1 < t_2 < \dots < t_k \\ \lambda_1, \dots, \lambda_k \in \mathbb{R}^d}} \sum_{\ell=1}^k [\langle \lambda_\ell, \phi(t_\ell) - \phi(t_{\ell-1}) \rangle - (t_\ell - t_{\ell-1})\Lambda(\lambda_\ell)] \\ &\geq \sup_{\substack{0 \leq s_1 < t_1 \leq s_2 < t_2 \leq \dots \leq s_k < t_k \\ \lambda_1, \dots, \lambda_k \in \mathbb{R}^d}} \sum_{\ell=1}^k [\langle \lambda_\ell, \phi(t_\ell) - \phi(s_\ell) \rangle - (t_\ell - s_\ell)\Lambda(\lambda_\ell)]. \end{aligned}$$

Hence, for $t_\ell = t_\ell^n$, $s_\ell = s_\ell^n$, and λ_ℓ proportional to $\phi(t_\ell) - \phi(s_\ell)$ and with $|\lambda_\ell| = \rho$, the following bound is obtained:

$$\begin{aligned} I_{\mathcal{X}}(\phi) &\geq \\ \limsup_{n \rightarrow \infty} \left\{ \rho \sum_{\ell=1}^{k_n} |\phi(t_\ell^n) - \phi(s_\ell^n)| - \left[\sup_{|\lambda|=\rho} \Lambda(\lambda) \right] \sum_{\ell=1}^{k_n} (t_\ell^n - s_\ell^n) \right\} &\geq \rho\delta. \end{aligned}$$

15. Page 157, proof of Lemma 5.1.14: The argument is incomplete, for one could have both sides of the equality before last in the page infinite when $\nu((-\infty, \bar{x})) > 0$. Rather, after (5.1.15), for any $M < \bar{x}$ such that $\nu((-\infty, M]) > 0$ integration by parts yields

$$\int_M^{\bar{x}} \frac{\nu(dx)}{\nu((-\infty, x])^\delta} \leq \frac{1}{1-\delta}.$$

Using monotone convergence, one may then set $M = -\infty$.

16. Page 161, line 11: Replace $\dot{g}^2(t)$ by $|\dot{g}(t)|^2$.
17. Page 161, line 14 and Page 163, line 9: Replace $\dot{\phi}^2(t)$ by $|\dot{\phi}(t)|^2$.
18. Page 161, line 10 and Page 163, line 12: add “all absolutely continuous functions with value 0 at 0 ...”
19. Page 164, (5.2.15): the right hand side should be $2e^{-(\delta-E)^2/2V}$, where

$$V = \sup_{0 \leq s, t \leq 1} E|X_{t,s}|^2.$$

20. Page 189, display in remark: add) before the transpose sign in the expression for $I_x(f)$.
21. Page 192, line -6: Replace $|y^2|$ by $|y|^2$.
22. Page 208, line 7: Replace $x \in G$ by $x \in B_\rho$.

23. Page 216, line 6: omit $-$.
24. Page 242, line 14: Add “is weakly” before “closed”.
25. Page 250, line 9 and in (6.3.7): replace N by N' .
26. Page 283, line 9: replace \mathcal{X} by \mathcal{Y} .
27. Page 298, line -9, remove one) before the period.
28. Page 313, line 11: replace “were” by “where”.
29. Page 322, line 11: add $f(t, x) : [0, \infty) \times \mathbb{R}^d \rightarrow \mathbb{R}^d$.
30. Page 331, item [KK86]: replace “Kellenberg” by “Kallenberg”.