EXERCISE 8 IN INTRODUCTION TO REPRESENTATION THEORY

DMITRY GOUREVITCH

- (1) Show that any subgroup and quotient group of a c-solvable group is c-solvable. Show that any finite nilpotent group is c-solvable.
- (2) (P) Suppose we know that a group G has a commutative normal subgroup N such that the group G/N is c-solvable. Show that any irreducible representation σ of G is monomial.
- (3) (P) Let G be a finite group, Z its central subgroup and χ a character of Z. Denote by $Irr(G)_{\chi}$ the set of equivalence classes of irreducible representations of G on which Z acts via the character with the central character χ .

 - (a) Compute Σ_{σ∈Irr(G)_χ} dim² σ.
 (b) Explain how to find the size of the set Irr(G)_χ. In particular show that this size is maximal when χ is a trivial character.

URL: http://www.wisdom.weizmann.ac.il/~dimagur/RepTheo4.html

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